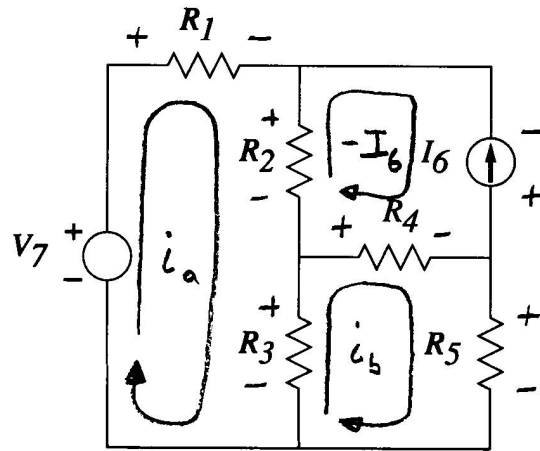


The first steps are to label the loop currents (to allow solution by the loop method) and to label each element with +/- signs (so we can talk about branch currents, voltages).



Next, we write KVL around each loop with unknown current. This can be done "by inspection":

$$i_a: (R_1 + R_2 + R_3) i_a - R_3 i_b = -R_2 I_6 + V_7$$

$$i_b: -R_3 i_a + (R_3 + R_4 + R_5) i_b = -R_4 I_6$$

Plugging in values, we have that

$$8 i_a - 3 i_b = -7$$

$$-3 i_a + 7 i_b = -15$$

This 2x2 set of equations can be solved by Cramer's rule, etc., to obtain

$$i_a = -2 A$$

$$i_b = -3 A$$

The branch currents are just the algebraic sum of loop currents:

$$i_1 = +i_a = -2 A$$

$$i_2 = i_a + I_c = 3 A$$

$$i_3 = i_a - i_b = 1 A$$

$$i_4 = i_b + I_c = 2 A$$

$$i_5 = i_b = -3 A$$

$$i_6 = I_c = 5 A$$

$$i_7 = -i_a = 2 A$$

The voltages are found by applying the constitutive laws:

$$v_1 = i_1 R_1 = -6 V$$

$$v_2 = i_2 R_2 = 6 V$$

$$v_3 = i_3 R_3 = 3 V$$

$$v_4 = i_4 R_4 = 6 V$$

$$v_5 = i_5 R_5 = -3 V$$

$$v_7 = v_7 = 3 V$$

Note that the constitutive law for the current source,

$$i_6 = I_6, \text{ for all } v_6$$

gives no information about  $v_6$ . To find  $v_6$ , apply KVL around  $I_6$  loop:

$$-v_4 - v_2 - v_6 = 0$$

$$\Rightarrow v_6 = -v_2 - v_4 = -12V$$

$$\boxed{v_6 = -12V}$$

Of course, these values agree with those of S3.

