

Introduction to Computers and Programming

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Lecture 4
Mar 17 2004

Data Structures*

- Example: Sorting elements
 - Input: a set S of numbers
 - Output: elements of S in increasing order
 - Algorithm:
 1. Locate smallest item in S
 2. Output smallest item
 3. Delete smallest item from S
 4. GOTO 1, while $S \neq \emptyset$

Key to a good solution: **data structure for S**

Topics for next 5 lectures

- Elementary data structures
 - Stacks and Queues
 - Linked lists
 - Graphs
 - Trees
- Today:
 - Stacks and Queues
 - FIFO vs. LIFO
 - Implementations using **arrays**
 - Expression Conversion

Stacks and Queues

- Dynamic sets in which the element removed from the set by the *Delete operation* is prespecified.
- **STACK**
 - Element deleted is: **most recently inserted element**
- **QUEUE**
 - Element deleted is: **element that has been in the set the longest**

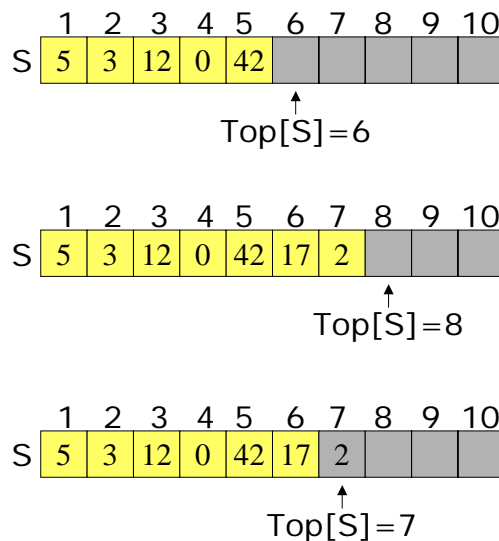
Stack

- **Stack**: A list with *insertion* and *deletion* both take place at **one** end: the top
 - Main operations
 - **Push**
 - New item added on top of stack, size of stack increases by one
 - **Pop**
 - Top-item removed from stack, decreasing stack size by one
 - Other operations
 - Initialize, Empty, Size, Top, Stack_Top, Display, ...
- Implements a **LIFO** policy
 - New **addition** makes older items inaccessible

Stack

- Example use of stacks:
- Implementations used:
 - Arrays or linked lists

Implementing Stack using Array



Empty(S)

```
if top[S]=1 then  
    return true  
else  
    return false
```

Push (S, x)

```
if STACK-FULL( $S$ ) then
    error "overflow"
else
     $S[top[S]] := x$ 
     $top[S] := top[S] + 1$ 
```

Pop (S)

```
if STACK-EMPTY( $S$ ) then
    error "underflow"
else
     $top[S] := top[S] - 1$ 
    return  $S[top[S]]$ 
```

my_stack.adb
my_stack.adb
test_stack.adb

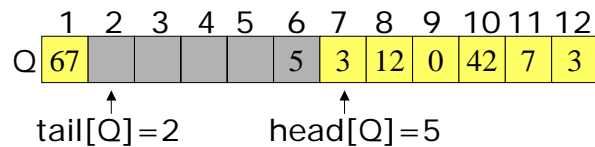
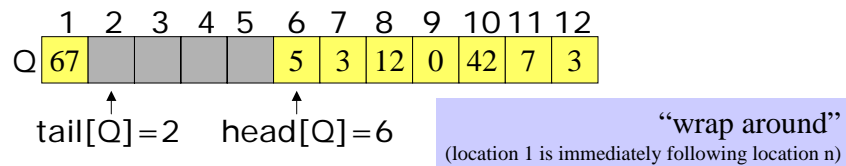
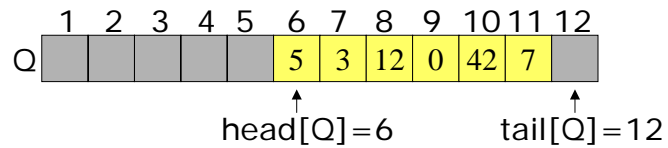
Performance and Limitations of My_Stack

- Performance
 - Let N be the number of elements in the stack
 - The space used is $O(N)$
 - Each operation used is $O(1)$
- Limitations
 - The maximum size of the stack must be defined a priori and cannot be changed
 - Trying to push a new element into a full stack causes an implementation-specific exception

Queue

- A list of elements with
 - Insertion: at end of list, tail
 - Deletion: at start of list, head
- Implements a **FIFO** policy
 - Queues are fair when someone has to wait
- Examples:

Implementing a Queue using an Array $Q[1..12]$



ENQUEUE (Q, x)

```

Q[tail[Q]] := x
if tail[Q] = length[Q] then
    tail[Q] := 1
else
    tail[Q] := tail[Q] + 1
    
```

DEQUEUE (Q)

```

x := Q[head[Q]]
if head[Q] = length[Q] then
    head[Q] := 1
else
    head[Q] := head[Q] + 1
return x
    
```

Operations on Queues

- Create, Enqueue, Dequeue, Size, Is_Empty, Is_Full, Display

Exercise: Update my_queue to make it a circular queue

my_queue.ads
my_queue.adb
test_queue.adb

Examples Using Stacks

- Infix vs. postfix
 - How to evaluate postfix
 - How to evaluate infix
- Convert Infix to Postfix

```
my_expression_converter.ads  
my_expression_converter.adb  
converter_test.adb  
[use these for this weeks PSET]
```

Infix vs. Postfix

Infix Expressions	Corresponding Postfix
$5 + 3 + 4 + 1$	$5 3 + 4 + 1 +$
$(5 + 3) * 10$	$5 3 + 10 *$
$(5 + 3) * (10 - 4)$	$5 3 10 4 - *$
$5 * 3 / (7 - 8)$	$5 3 * 7 8 - /$
$(b * b - 4 * a * c) / (2 * a)$	$b b * 4 a * c * - 2 a * /$

How to Evaluate Postfix

A program can evaluate postfix expressions by reading the expression from left to right

```
for I in 1 .. length loop  
  If Is_Number(expr(I)) = true then  
    push expr(I)  
  If Is_Operator(expr(I)) then  
    pop two numbers from the stack  
    perform operation  
    push result onto stack  
end loop  
-- result is on top of stack
```

How is a bad postfix expression indicated?

Evaluating infix expressions

- Need two stacks, one for numbers and one for operators

```
for I in 1 .. length loop  
  If Is_Number(expr(I)) = true then  
    push expr(I) onto operand_stack  
  If Is_Operator(expr(I)) then  
    push expr(I) onto operator_stack  
  If expr(I) = ')' then  
    pop 2 numbers from operand_stack  
    pop an operator from the operator_stack  
    perform operation  
    push the result onto the operand_stack  
end loop  
-- The top of stack contains the result.
```

Infix to Postfix: Example

- Infix Expression

3 + 5 * 6 - 7 * (8 + 5)

- Postfix Expression

3 5 6 * + 7 8 5 + * -

Infix to Postfix

```
post_fix := ""
Create(Op_Stack)
for I in 1 .. Length loop
    If Is_Operand(expr(I)) = true then
        Append(post_fix, expr(I))

    If Is_Operator(expr(I)) = true then
        Process_Next_Operator(expr(I))
end loop
-- string post_fix has the result
```

Process_Next_Operator

Done := False

loop

If Is_Empty(Op_Stack) **or** next_op is '(',

 push next_op onto Op_Stack

 set Done to True

Elsif precedence(next_op) > precedence(top_operator)

 Push next_op onto Op_stack

 -- ensures higher precedence operators evaluated first

 Set Done to True

Else

 Pop the operator_stack

If operator popped is '(',

 set Done to True

Else

 append operator popped to post_fix string

exit when Done = True

end loop