

AERO | ASTRO



16.682 - Prototyping Avionics Spring 2006

Lecture 2

February 13, 2006

DEPARTMENT OF AERONAUTICS AND ASTRONAUTICS

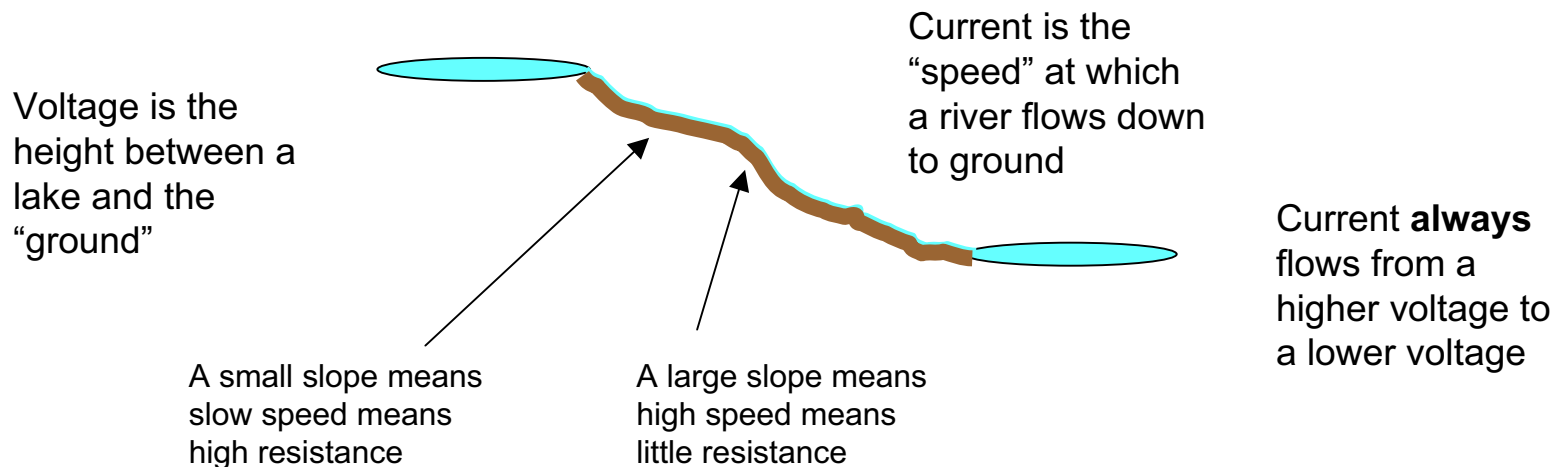
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Outline

- **Voltage and Current**
- **4 basic “component laws”**
- **2 basic “network laws”**
- **Resistors**
- **Capacitors**
- **Inductors**

Voltage & Current

- Any electronic project depends at the most basic level on:
 - Voltage
 - The electric potential difference between two points
 - Like “potential energy” of physics
 - Current
 - The flow of electricity through components and wires
 - Like “kinetic energy” of physics
- There are many ways people think about current and voltage, most involve a fluid like water, here is an example:



Components

- **The most basic components of an electronic circuit are:**

- **Resistor**

- Resistance is an inherent property of all materials
- Conductive materials have small resistance, non-conductive high resistance
- Wire is an approximately 0Ω resistor
- Purely a passive element
- Like the “slope” of the mountain

- **Capacitor**

- Stores energy: as current flows in the capacitor charges in voltage, as current flows out it discharges
- Like a small intermediate “lake” in the mountain

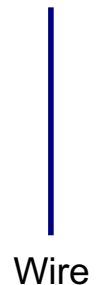
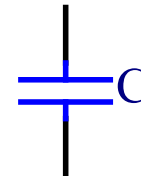
- **Inductor**

- Stores energy: as voltage is applied, it makes current flow faster, as voltage goes down the current slows
- Like a local “increase in gravity” in the mountain

Resistor (R)



Capacitor (C)



Inductor (L)



Units and Common Values

Description	Units	Symbol	Typical Values
Voltage	Volts	V	1mV → 10kV
Current	Ampere	A	1 μ A → 10A
Resistance	Ohms	Ω	1m Ω → M Ω
Capacitance	Farad	F	1 μ F → 1mF
Inductance	Henry	H	1mH → 1H

Component Laws

- The most basic “laws” for these components are:

- Resistor

$$V = IR \leftrightarrow I = \frac{V}{R} \leftrightarrow R = \frac{V}{I}$$

$$P = IV \leftrightarrow P = I^2 R \leftrightarrow P = \frac{V^2}{R}$$

- Capacitor

$$i = C \frac{dv}{dt}$$

- Inductor

$$v = L \frac{di}{dt}$$

- *Capacitors and Inductors are “dual” or each other*

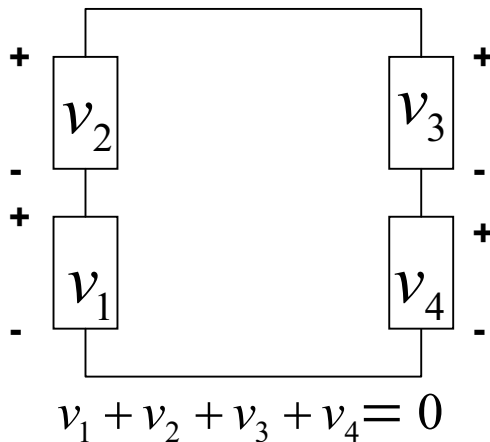
- *What one does with voltage, the other does with current*

Network Laws

- A circuit is full of *nodes* and *loops*
 - The Kirchhoff Voltage Law (KVL) and Current Law (KCL) tell you how to figure out the voltage and current in a circuit

$$\sum_L v_l = 0$$

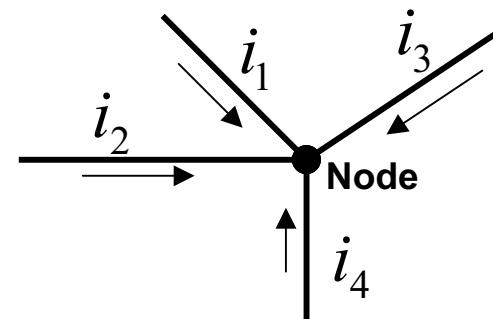
- *The sum of all voltages around a loop must be 0*



Note: at least one voltage must be negative (the +/- signs are backwards)!

$$\sum_N i_n = 0$$

- *The sum of all currents into a node must be 0*

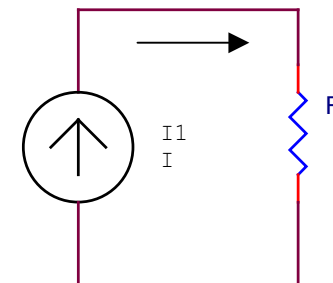
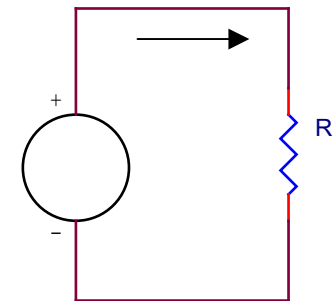
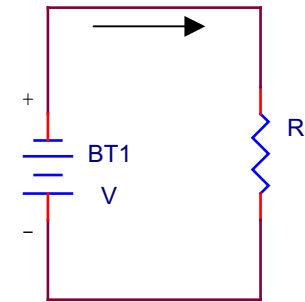


$$i_1 + i_2 + i_3 + i_4 = 0$$

Note: at least one current must be negative (flow opposite of the arrow)!

Supplies

- **To make circuit analysis possible, we use models of voltage and current supplies:**
 - **Voltage supplies provide constant voltage and any necessary current**
 - **Current flows out of the positive side, through the circuit, and back into the negative side of a supply**
 - **Current supplies provide constant current in the direction of the arrow and work at any necessary voltage**



Basic Circuits

- **Node analysis: KCL**

- $i_0 = i_R + i_C$

- $$i_0 = \frac{v}{R} + C \frac{dv}{dt}$$

- $$v + RC \frac{dv}{dt} = i_0 R$$

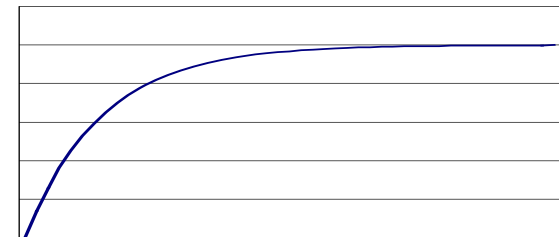
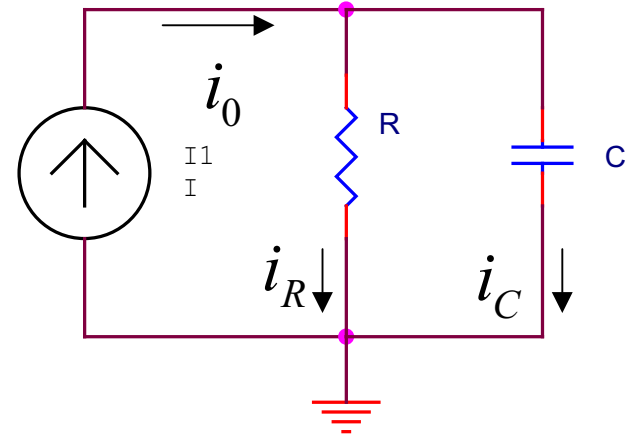
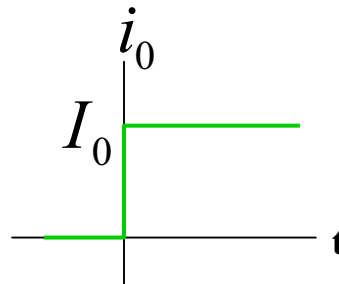
- Resistor/Capacitor circuits will always have a *time constant* of RC!

- **Actual response depends on input current**

- Example: $i_0 =$ step function

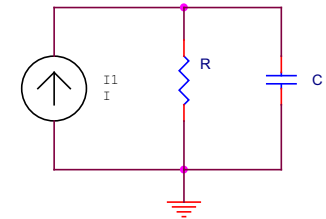
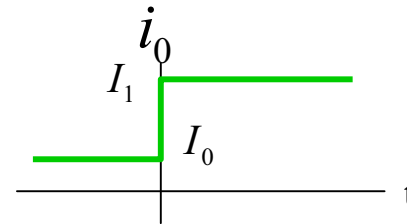
$$V = I_0 R \left(1 - e^{-\frac{t}{RC}} \right)$$

time constant!



ZIR and ZSR

- Solving circuits with inductors/capacitors is easiest if you use super-position to add the
 - Zero Input Response
 - The behavior which depends only on the “state” of the capacitor/inductor at time zero, without any change in the input
 - Zero State Response
 - The behavior which depends only on the response of the capacitor/inductor due to a change in the input



ZIR :

$$t < 0, v = I_0 R$$

$$t > 0, i = C \frac{dv}{dt} \rightarrow v + RC \frac{dv}{dt} = 0$$

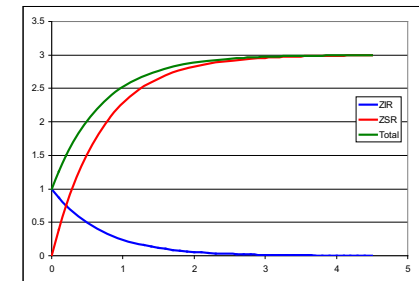
$$\rightarrow v = I_0 R \cdot e^{-\frac{t}{RC}}$$

ZSR :

$$t < 0, v = 0$$

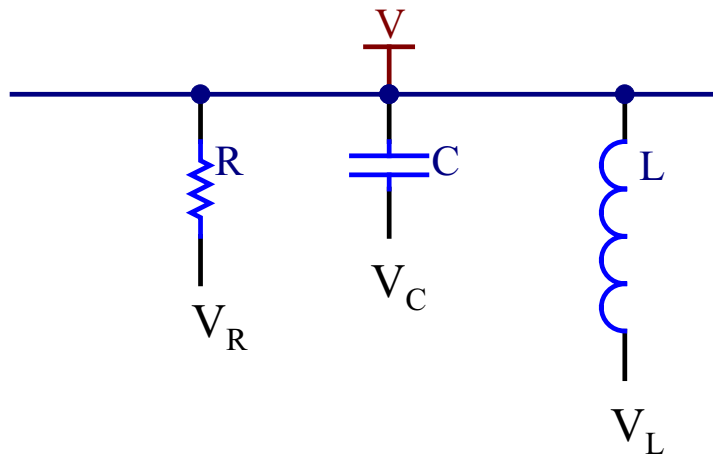
$$t > 0, i = C \frac{dv}{dt} \rightarrow v + RC \frac{dv}{dt} = I_1 R$$

$$\rightarrow v = I_1 R \left(1 - e^{-\frac{t}{RC}} \right)$$



Useful Clue

- From $v = iR$
 - What happens with unconnected ends of components?



- Because $i=0$ then v across are 0
 - $V_R=V$
 - $V_C=V$ *it is not floating!*
 - $V_L=V$