

# 5.73

## Quiz 27

$$\mathbf{T}_{\pm 1}^{(1)} = \mp 2^{-1/2} (\mathbf{x} \pm i\mathbf{y}), \quad \mathbf{T}_0^{(1)} = \mathbf{z}$$

$$[\mathbf{J}_i, \mathbf{q}_j] = i\hbar \sum_k \varepsilon_{ijk} \mathbf{q}_k$$

A. Show that  $[\mathbf{J}_z, \mathbf{T}_{-1}^{(1)}] = \hbar \mathbf{T}_{-1}^{(1)}$

B. Show that  $[\mathbf{J}_-, \mathbf{T}_{-1}^{(1)}] = 0$

C. If  $\mathbf{T}_{\mu}^{(\omega)}$  satisfies the  $[\mathbf{J}_{\pm}, \mathbf{T}_{\mu}^{(\omega)}] = \hbar[\omega(\omega+1) - \mu(\mu \pm 1)]^{1/2} \mathbf{T}_{\mu \pm 1}^{(\omega)}$  and  $[\mathbf{J}_z, \mathbf{T}_{\mu}^{(\omega)}] = \hbar\mu \mathbf{T}_{\mu}^{(\omega)}$  definitions, then we are supposed to know all selection rules for matrix elements of  $\mathbf{T}_{\mu}^{(\omega)}$  in the  $|JM_J\rangle$  basis set. What are the  $\Delta J$  and  $\Delta M_J$  selection rules for  $\mathbf{T}_{+2}^{(3)}$ ?

$$\Delta J = \quad \Delta M_J =$$

(over)

- D. Show that the operator  $(\mathbf{L}_+)^2$  satisfies at least one part of the commutation rule definition for  $\mathbf{T}_{+2}^{(2)}$ :  $[\mathbf{J}_z, \mathbf{T}_2^{(2)}] = \hbar 2 \mathbf{T}_2^{(2)}$ .

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