

**6.002**

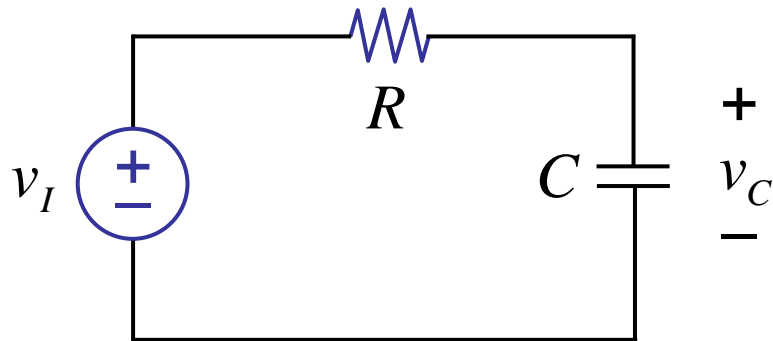
**CIRCUITS AND  
ELECTRONICS**

# State and Memory

Cite as: Anant Agarwal and Jeffrey Lang, course materials for 6.002 Circuits and Electronics, Spring 2007. MIT OpenCourseWare (<http://ocw.mit.edu/>), Massachusetts Institute of Technology. Downloaded on [DD Month YYYY].

# Review

## Recall



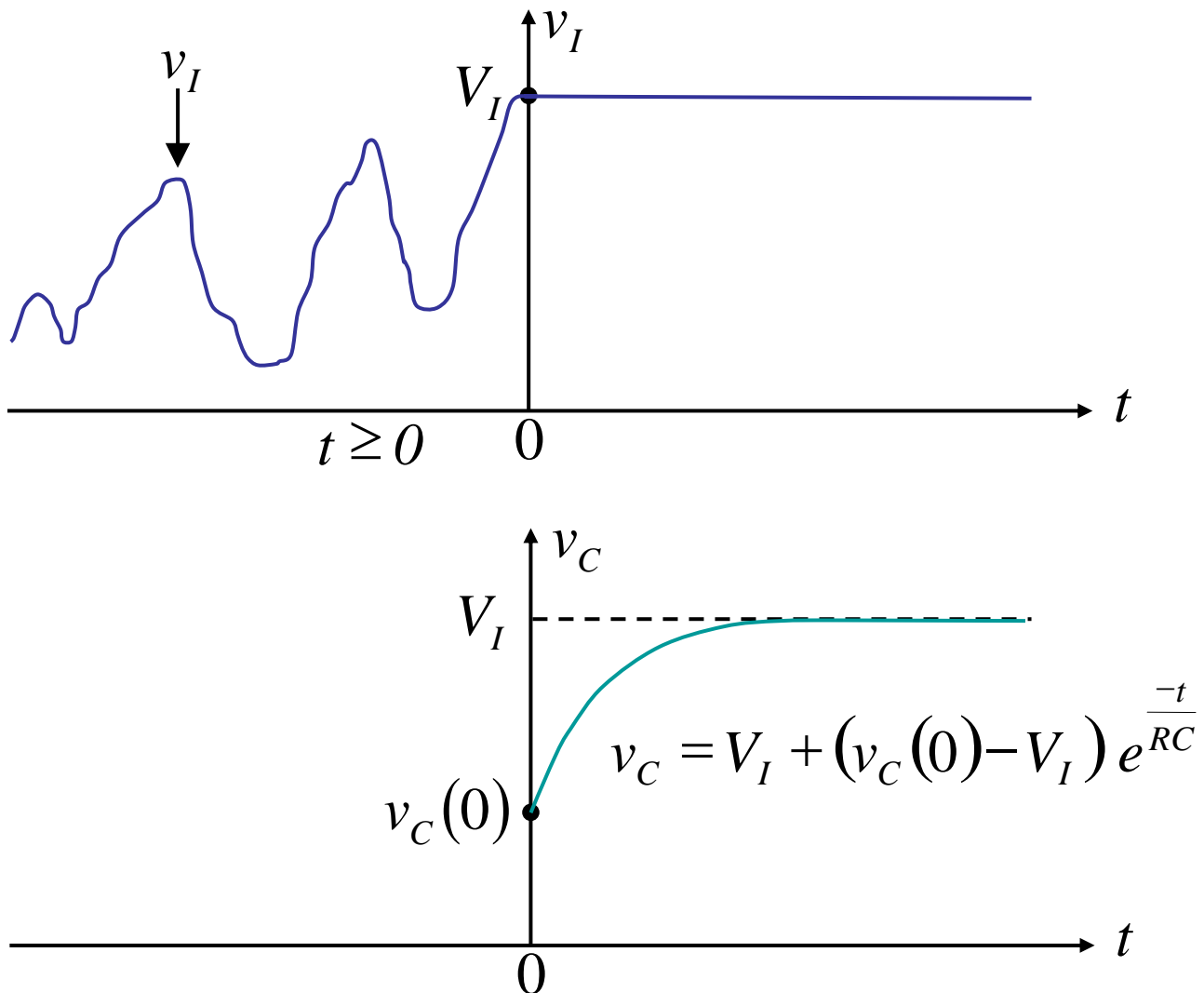
$$v_I = V_I \quad \text{for} \quad t \geq 0 \qquad v_C(0)$$

$$v_C = V_I + (v_C(0) - V_I) e^{\frac{-t}{RC}} \quad \text{---} \quad \textcircled{1}$$

**Reading:** Sections 10.3, 10.5, and 10.7

# This lecture will dwell on the memory property of capacitors.

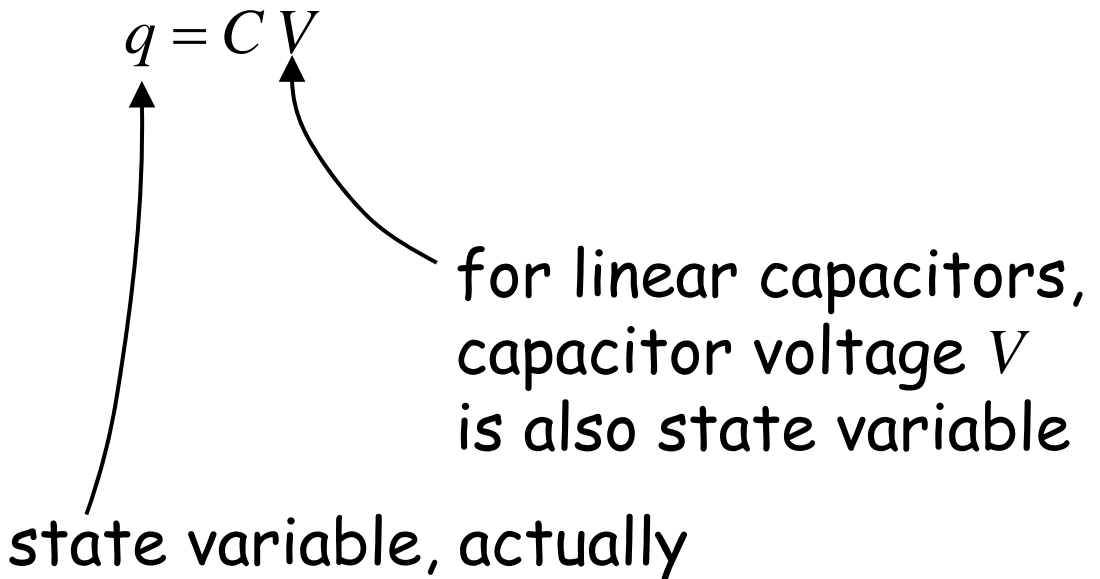
For the RC circuit in the previous slide



Notice that the capacitor voltage for  $t \geq 0$  is independent of the form of the input voltage before  $t = 0$ . Instead, it depends only on the capacitor voltage at  $t = 0$ , and the input voltage for  $t \geq 0$ .

# State

***State*** : summary of past inputs relevant to predicting the future



# State

Back to our simple RC circuit ①

$$v_C = f(v_C(0), v_I(t))$$

$$v_C = V_I + (v_C(0) - V_I) e^{\frac{-t}{RC}}$$



Summarizes the past input relevant to predicting future behavior

# State

We are often interested in circuit response for

- zero state  $v_C(0) = 0$
- zero input  $v_I(t) = 0$

Correspondingly,

- zero state response or *ZSR*

$$v_C = V_I - V_I e^{\frac{-t}{RC}} \quad \text{—————} \quad \textcircled{2}$$

- zero input response or *ZIR*

$$v_C = v_C(0) e^{\frac{-t}{RC}} \quad \text{—————} \quad \textcircled{3}$$

# One application of STATE



## DIGITAL MEMORY

Why memory?

Or, why is combinational logic insufficient?

### Examples

- Consider adding 6 numbers on your calculator

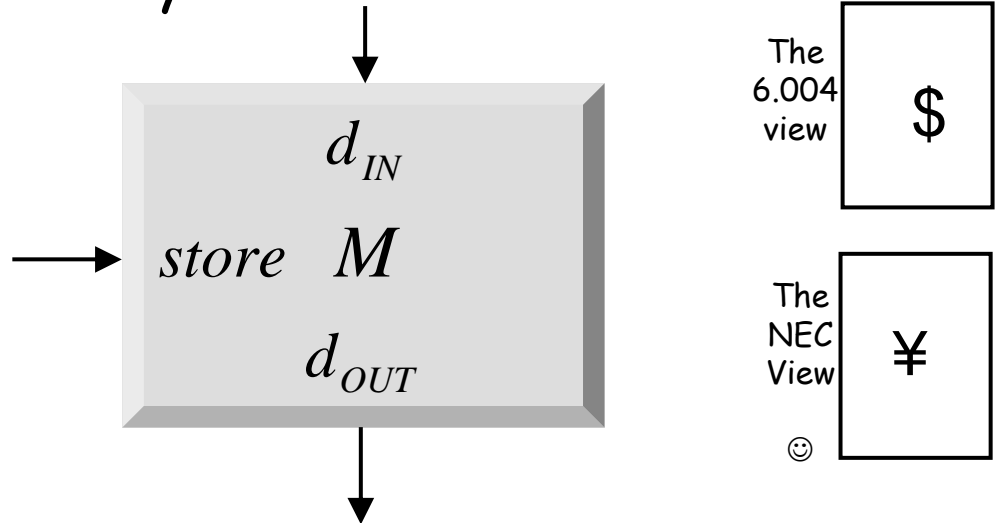
$$2 + 9 + 6 + 5 + 3 + 8$$



- "Remembering" transient inputs

# Memory Abstraction

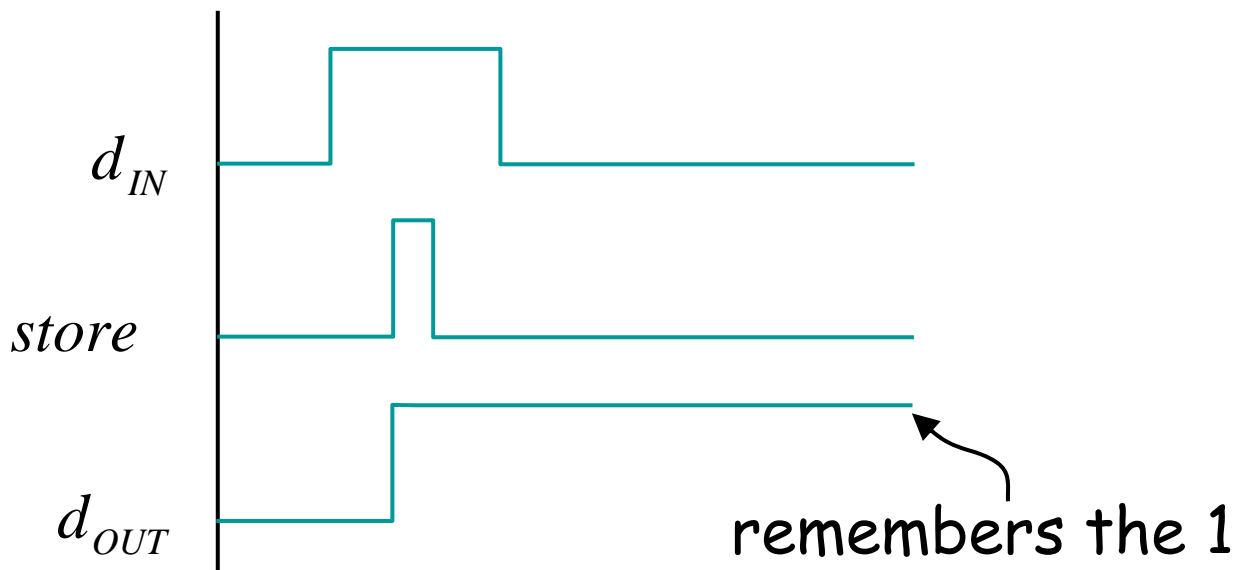
A 1-bit memory element



Remembers input when *store* goes high.

Like a camera that records input ( $d_{IN}$ ) when the user presses the shutter release button.

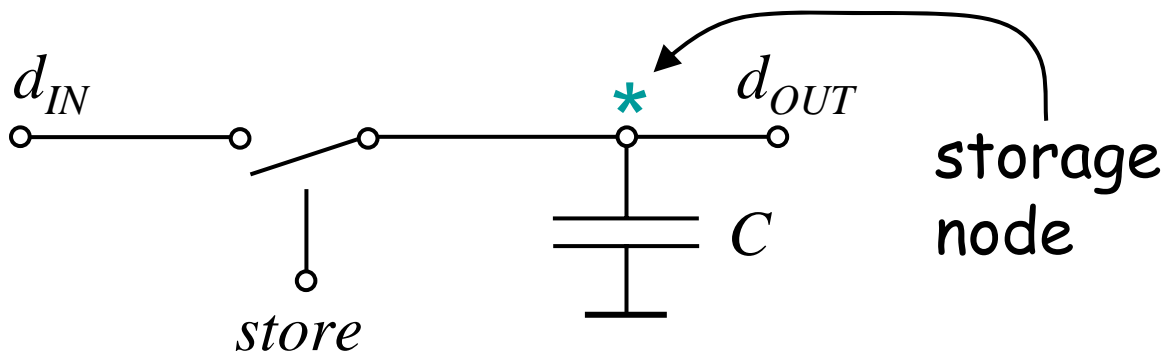
The recorded value is visible at  $d_{OUT}$ .





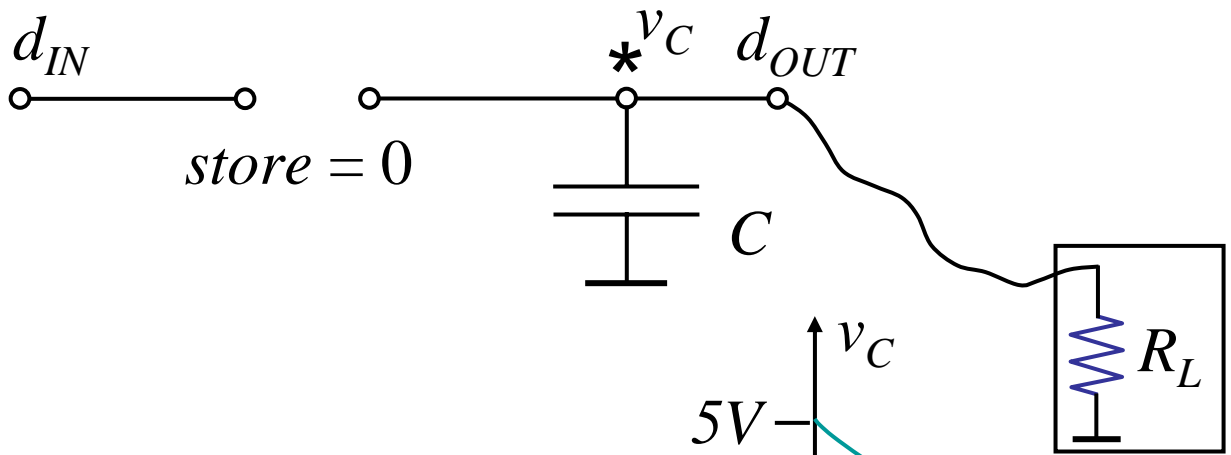
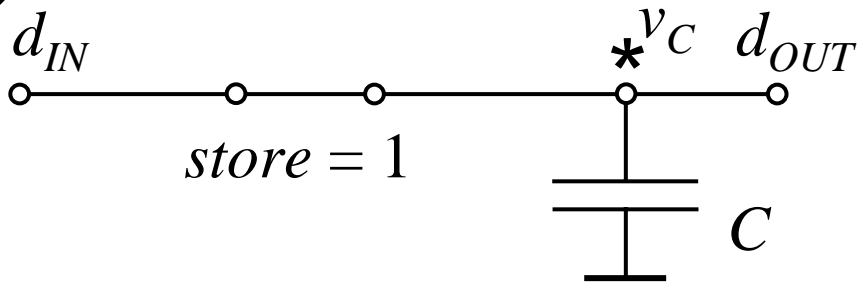
# Building a memory element ...

## Ⓐ First attempt

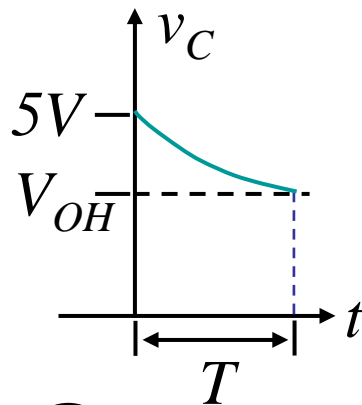


# Building a memory element ...

(A)



Stored value leaks away



$$v_C = 5 \cdot e^{\frac{-t}{R_L C}}$$

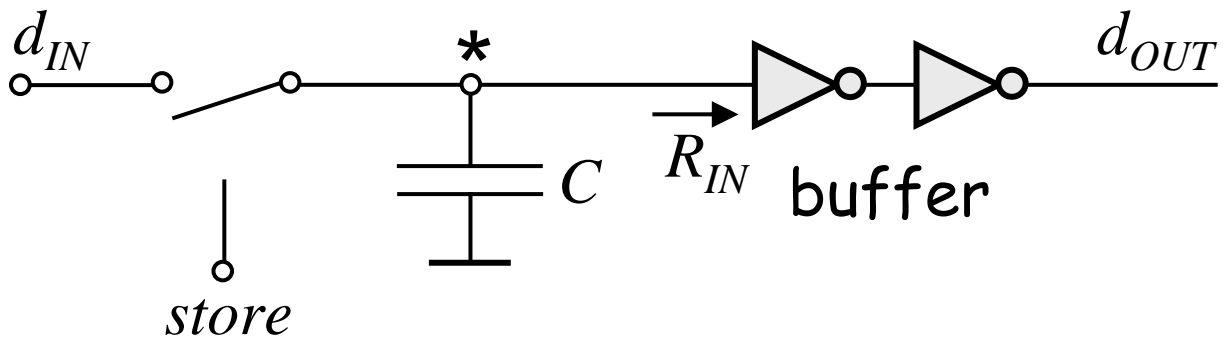
from (2)

$$T = -R_L C \ln \frac{V_{OH}}{5}$$

store pulse width  $\gg R_{ON} C$

# Building a memory element ...

(B) Second attempt → buffer



Input resistance  $R_{IN}$

$$T = -R_{IN} C \ln \frac{V_{OH}}{5}$$

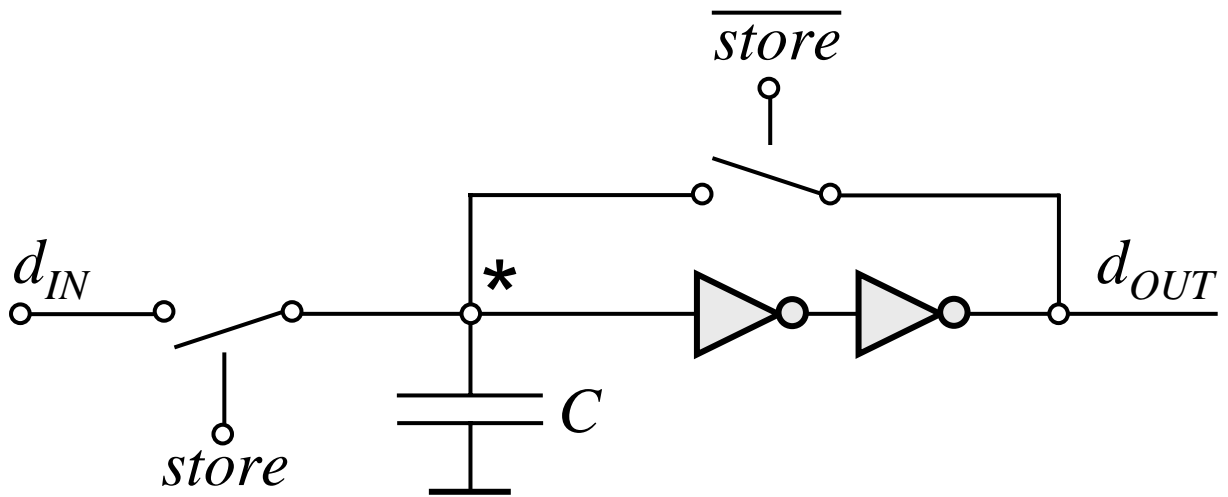
$$R_{IN} \gg R_L$$

Better, but still not perfect.



# Building a memory element ...

③ Third attempt → buffer + refresh

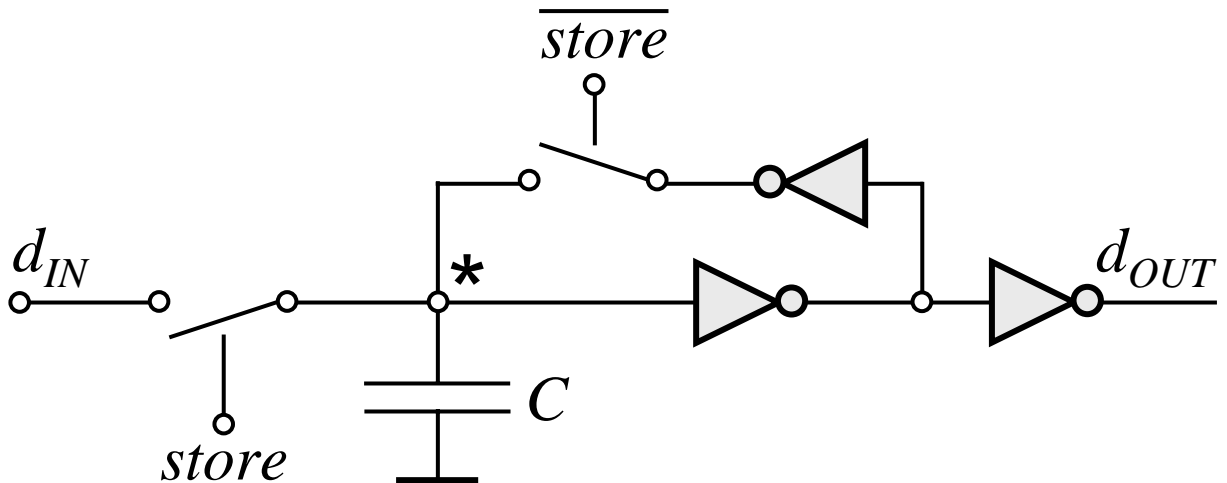


Does this work?

No. External value can influence storage node.

# Building a memory element ...

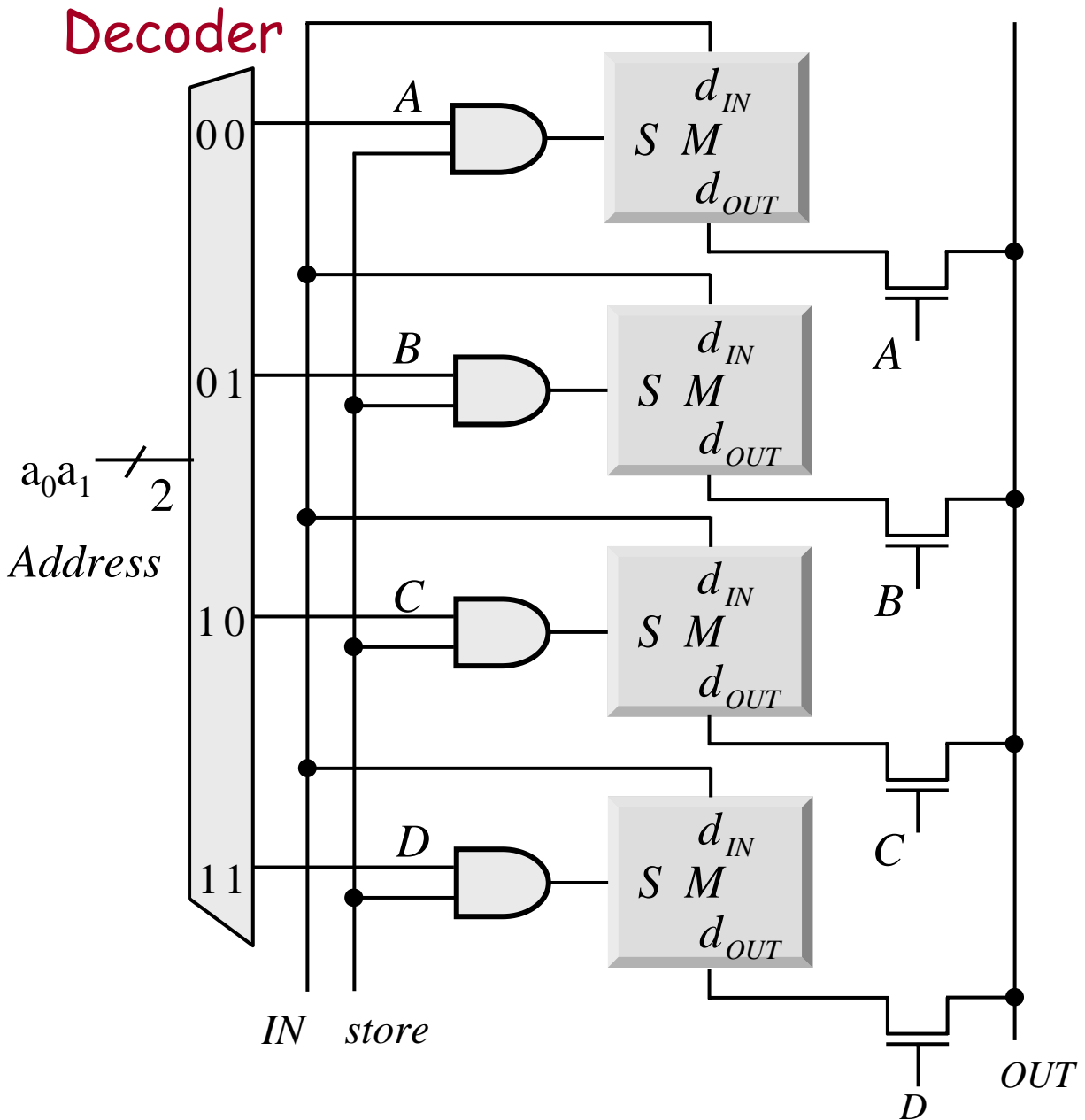
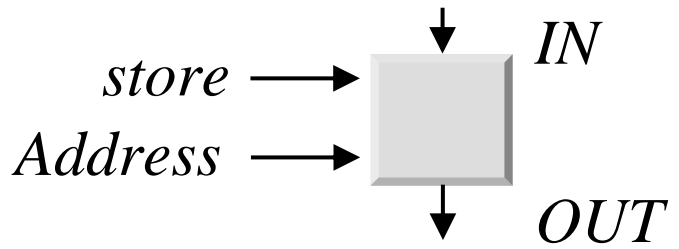
④ Fourth attempt → buffer + decoupled refresh



Works!

# A Memory Array

4-bit memory



## Truth table for decoder

$a_0$	$a_1$	$A$	$B$	$C$	$D$
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

## Agarwal's top 10 list on memory

- 10 I have no recollection, Senator.
- 9 I forgot the homework was due today.
- 8 Adlibbing  $\equiv$  ZSR
- 7 I think, therefore I am.
- 6 I think that was right.
- 5 I forgot the rest ...