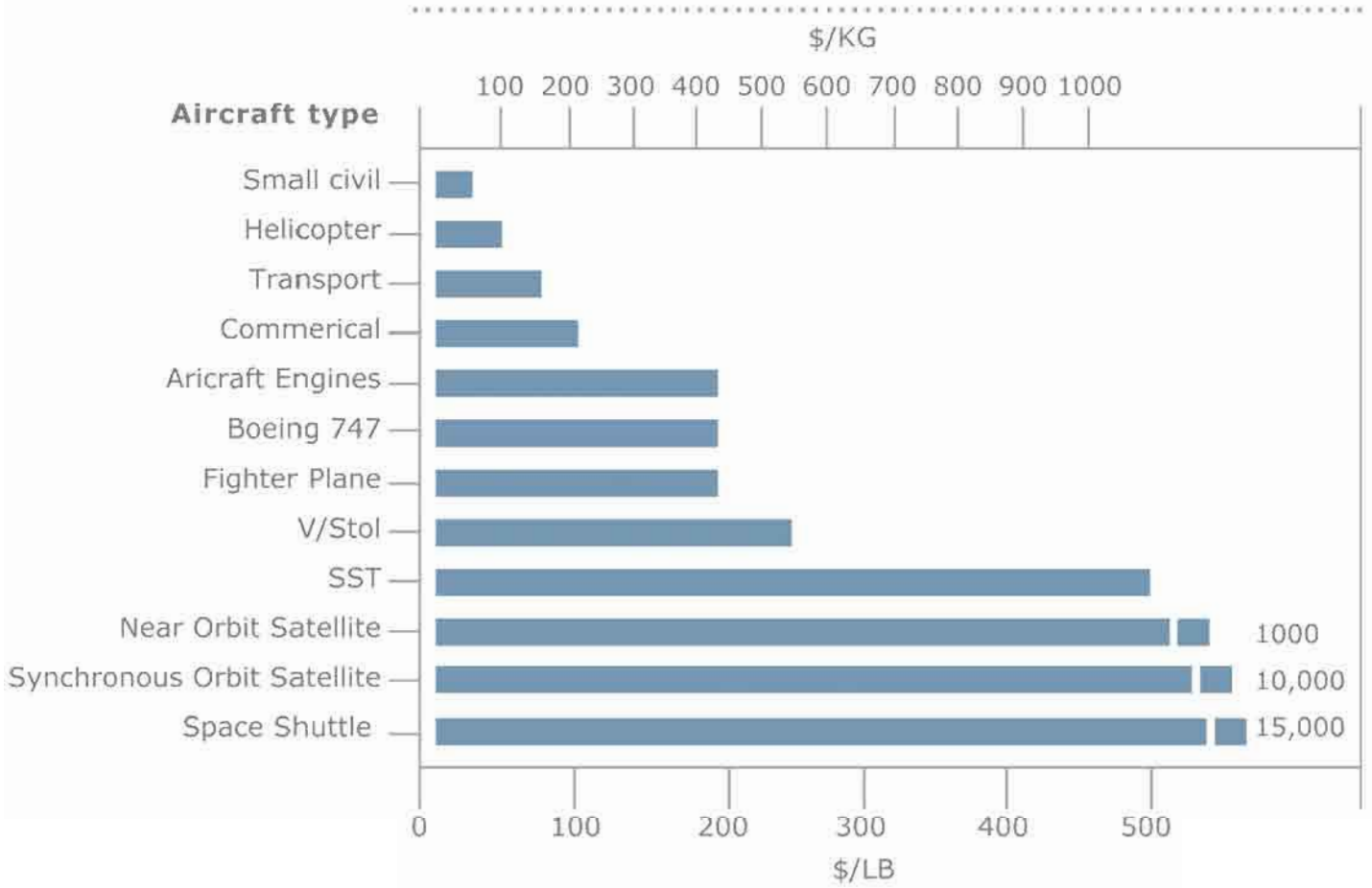
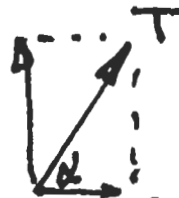
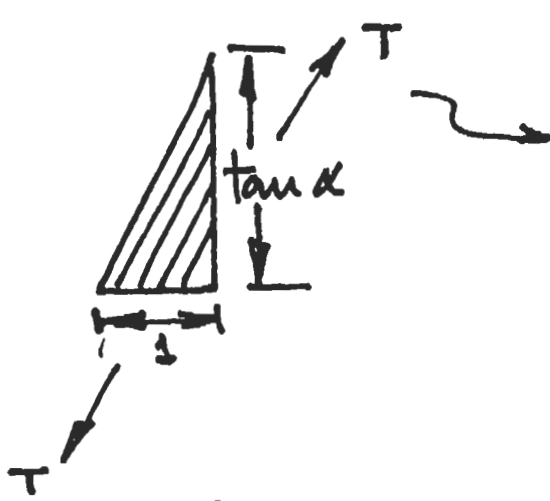
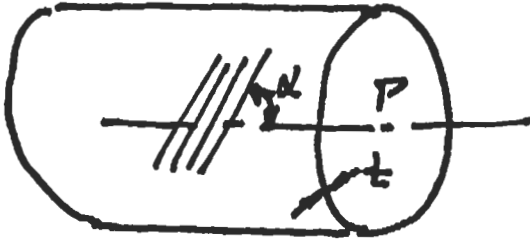


### Value of weight saved in aircraft and spacecraft



# Netting Analysis - balanced pattern



$$\frac{nT \cos \alpha}{(\tan \alpha)(t)} = \frac{P_r}{2t} \quad (1)$$



$$\frac{nT \sin \alpha}{(1)(t)} = \frac{P_r}{t} \quad (2)$$

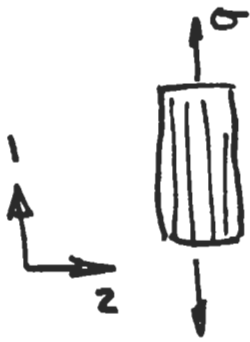
$$\frac{(2)}{(1)} \Rightarrow \frac{nT \sin \alpha \cdot \tan \alpha}{t \cdot nT \cos \alpha} = \frac{P_r/t}{P_r/2t} = 2$$

$$\rightarrow \tan^2 \alpha = 2$$

$$\alpha = \tan^{-1} \sqrt{2} = 54.4^\circ$$

# Micromechanics of Laminates

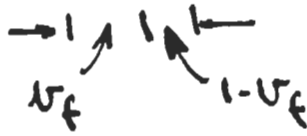
## • Parallel reinforcement



$$E_f = E_m = E$$

$$P_f + P_m = P$$

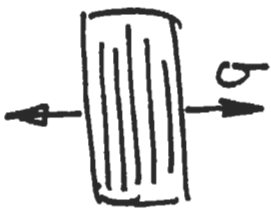
$$\sigma_f V_f + \sigma_m V_m = \sigma (1)$$



$\div E$

$$E_f V_f + E_m V_m = E_1$$

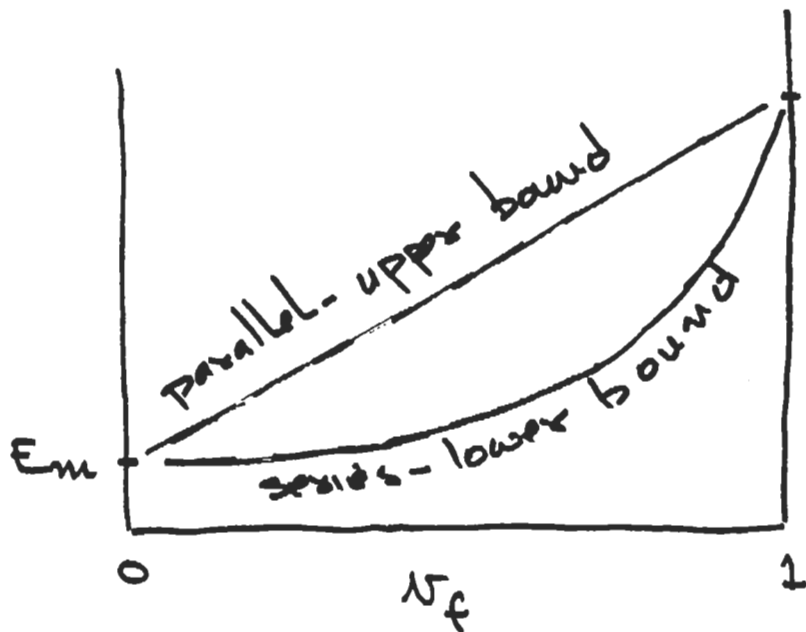
## • Series reinforcement



$$P_f = P_m = P$$

$$\delta_f + \delta_m = \delta$$

$$\frac{1}{E_2} = \frac{V_f}{E_f} + \frac{V_m}{E_m}$$



Kalpain-Tsai:

$$E_2 = E_m \frac{1 + \xi \eta V_f}{1 - \eta V_f}$$

$$\eta = \frac{\left(\frac{E_f}{E_m} - 1\right)}{\left(\frac{E_f}{E_m} + \xi\right)}$$

$\xi = \xi$  (geometry, packing)

• Strength - assume  $\epsilon_{b,m} > \epsilon_{b,f}$

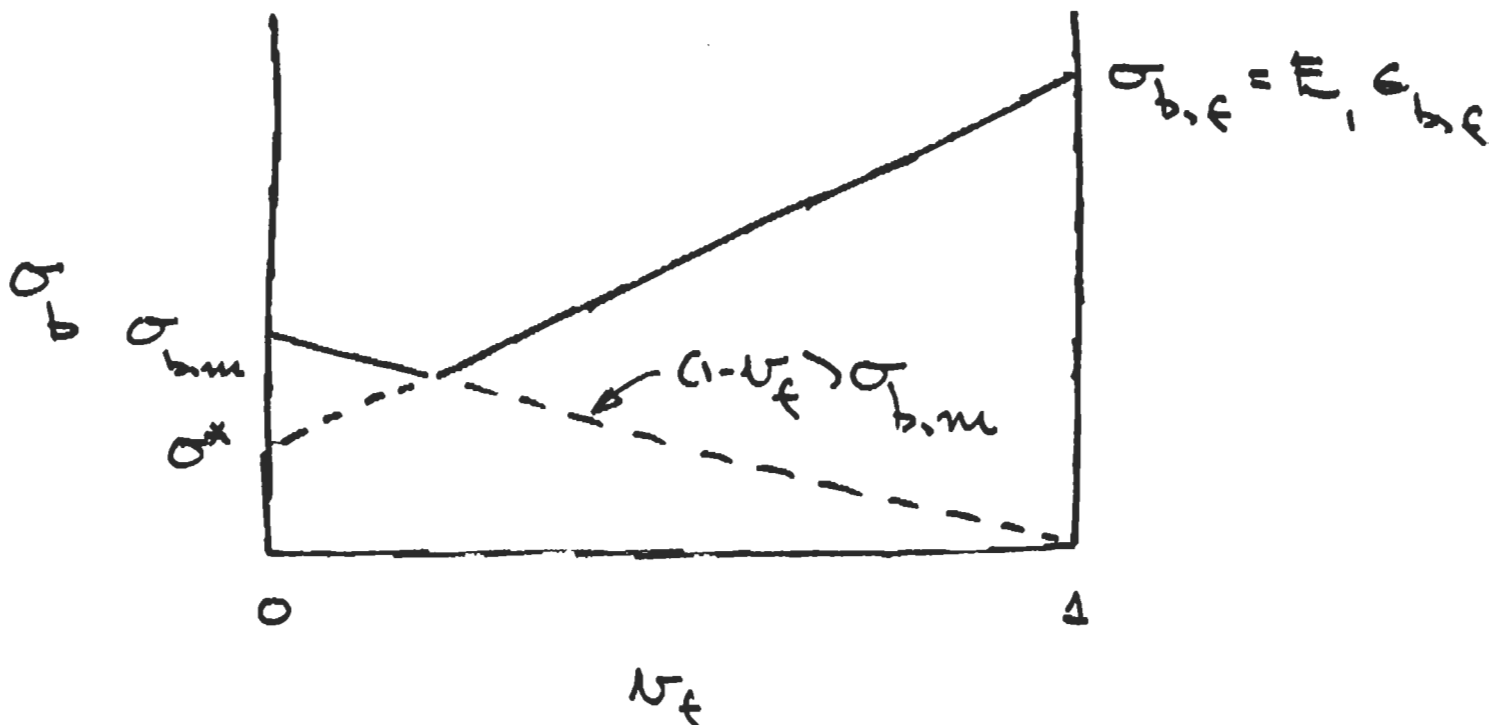
for rupture @  $\epsilon = \epsilon_{b,f}$ :

$$E_1 = v_f E_f + v_m E_m$$

$\times \epsilon$ :

$$\sigma_b = \epsilon_{b,f} E_1 = v_f \sigma_{b,f} + (1-v_f) \sigma^*$$

$$\sigma^* = \text{matrix stress} = \epsilon_{b,f} E_m$$



$$\sigma_{b,m} = E_m \epsilon_{b,m} = \text{breaking strength of matrix}$$